Instances of Schneider's generalized protocol of clock synchronization.

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Abstract

Schneider [7] generalizes a number of protocols for Byzantine fault-tolerant clock synchronization and presents a uniform proof for their correctness. In Schneider's schema, each processor maintains a local clock by periodically adjusting each value to one computed by a convergence function applied to the readings of all the clocks. Then, correctness of an algorithm, i.e. that the readings of two clocks at any time are within a fixed bound of each other, is based upon some conditions on the convergence function. To prove that a particular clock synchronization algorithm is correct it suffices to show that the convergence function used by the algorithm meets Schneider's conditions.

Using the theorem prover Isabelle, we formalize the proofs that the convergence functions of two algorithms, namely, the Interactive Convergence Algorithm (ICA) of Lamport and Melliar-Smith [4] and the Fault-tolerant Midpoint algorithm of Lundelius-Lynch [5], meet Schneider's conditions. Furthermore, we experiment on handling some parts of the proofs with fully automatic tools like ICS[3] and CVC-lite[2].

These theories are part of a joint work with Alwen Tiu and Leonor P. Nieto [1]. In this work the correctness of Schneider schema was also verified using Isabelle (available at http://isa-afp.org/entries/GenClock.shtml).

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1 Interactive Convergence Algorithms (ICA)

theory ICAInstance imports Complex-Main begin

This algorithm is presented in [4].

A proof of the three properties can be found in [8].

1.1 Model of the system

The main ideas for the formalization of the system were obtained from [8].

1.1.1 Types in the formalization

The election of the basics types was based on [8]. There, the process are natural numbers and the real time and the clock readings are reals.

```
{f type-synonym}\ process = nat {f type-synonym}\ time = real — real time {f type-synonym}\ Clocktime = real — time of the clock readings (clock time)
```

1.1.2 Some constants

Here we define some parameters of the algorithm that we use: the number of process and the fix value that is used to discard the processes whose clocks differ more than this amount from the own one (see [8]). The defined constants must satisfy this axiom (if np = 0 we have a division by cero in the definition of the convergence function).

axiomatization

```
np:: nat — Number of processes and \Delta:: Clocktime — Fix value to discard processes where constants-ax: <math>\theta <= \Delta \land np > \theta
```

We define also the set of process that the algorithm manage. This definition exist only for readability matters.

definition

```
PR :: process set  where [simp]: PR = \{... < np\}
```

1.1.3 Convergence function

This functions is called "Egocentric Average" ([7])

In this algorithm each process has an array where it store the clocks readings from the others processes (including itself). We formalise that as a function from processes to clock time as [8].

First we define an auxiliary function. It takes a function of clock readings and two processes, and return de reading of the second process if the difference of the readings is grater than Δ , otherwise it returns the reading of the first one.

definition

```
fiX :: [(process \Rightarrow Clocktime), process, process] \Rightarrow Clocktime where fiX f p l = (if | f p - f l | <= \Delta then (f l) else (f p))
```

And finally the convergence function. This is defined with the builtin generalized summation over a set constructor of Isabelle. Also we had to use the overloaded real function to typecast de number np.

definition

```
cfni :: [process, (process \Rightarrow Clocktime)] \Rightarrow Clocktime  where cfni \ p \ f = (\sum l \in \{... < np\}. \ fiX \ f \ p \ l) \ / \ (real \ np)
```

1.2 Translation Invariance property.

We first need to prove this auxiliary lemma.

lemma trans-inv':

```
(\sum l \in \{.. < np'\}. \ fiX \ (\lambda \ y. \ f \ y + x) \ p \ l) = \\ (\sum l \in \{.. < np'\}. \ fiX \ f \ p \ l) + real \ np' * x \\ \langle proof \rangle
theorem trans-inv:
\forall \ p \ f \ x \ . \ cfni \ p \ (\lambda \ y. \ f \ y + x) = cfni \ p \ f + x \\ \langle proof \rangle
```

1.3 Precision Enhancement property

An informal proof of this theorem can be found in [8]

1.3.1 Auxiliary lemmas

 $C \subseteq PR \Longrightarrow finite C$

lemma finitC:

 $\langle proof \rangle$

```
\mathbf{lemma}\ finitnpC\colon
  finite (PR - C)
\langle proof \rangle
The next lemmas are about arithmetic properties of the generalized sum-
mation over a set constructor.
{\bf lemma}\ sum-abs\text{-}triangle\text{-}ineq:
finite S \Longrightarrow
  |\sum l \in S. (f::'a \Rightarrow 'b::linordered-idom) l| <= (\sum l \in S. |f l|)
  (is ... \implies ?P S)
  \langle proof \rangle
lemma sum-le:
  \llbracket \textit{finite } S \text{ ; } \forall \text{ } r \in S. \textit{ } f \textit{ } r <= \textit{ } b \text{ } \rrbracket
  (\sum l \in S. \ f \ l) \le real \ (card \ S) * b
  (\overline{\mathbf{is}} \parallel finite S ; \forall r \in S. fr \le b \parallel \implies ?PS)
\langle proof \rangle
lemma sum-np-eq:
assumes
  hC: C \subseteq PR
shows
  (\sum l \in \{... < np\}. \ f \ l) \ = \ (\sum l \in C. \ f \ l) \ + \ (\sum l \in (\{... < np\} - C). \ f \ l)
\langle proof \rangle
lemma abs-sum-np-ineq:
assumes
  hC: C \subseteq PR
shows
  |(\sum l \in \{.. < np\}. (f::nat \Rightarrow real) l)| <=
```

```
(\sum l \in C. |f| l|) + (\sum l \in (\{.. < np\} - C). |f| l|)
(\mathbf{is} ?abs-sum <= ?sumC + ?sumnpC)
\langle proof \rangle
```

The next lemmas are about the existence of bounds that are necesary in order to prove the Precicion Enhancement theorem.

```
lemma fiX-ubound:
 fiX f p l \le f p + \Delta
\langle proof \rangle
lemma fiX-lbound:
 f p - \Delta \le fiX f p l
\langle proof \rangle
lemma abs-fiX-bound: |fiX f p l - f p| <= \Delta
lemma abs-dif-fiX-bound:
assumes
  hbx: \forall l \in C. |fl - ql| \le x \text{ and }
  hby: \forall l \in C. \forall m \in C. |fl - fm| \le y \text{ and }
  hpC: p \in C and
  hqC: q \in C
shows
  |fiX f p r - fiX g q r| \le 2 * \Delta + x + y
\langle proof \rangle
lemma abs-dif-fiX-bound-C-aux1:
assumes
  hbx: \forall l \in C. |fl - gl| \le x  and
  hby1: \forall l \in C. \forall m \in C. |fl - fm| \le y and
  hby2: \forall l \in C. \forall m \in C. |gl - gm| \le y and
  hpC: p \in C and
  hqC: q \in C and
  hrC: r \in C
shows
 |\mathit{fi}X\,f\,p\,\,r\,-\,\mathit{fi}X\,g\,\,q\,\,r|\,<=\,x\,+\,y
lemma abs-dif-fiX-bound-C-aux2:
assumes
 hbx: \forall l \in C. |fl - gl| \le x and
  hby1: \forall l \in C. \forall m \in C. |fl - fm| \le y \text{ and }
  hby2: \forall l \in C. \forall m \in C. |gl - gm| \le y and
  hpC: p \in C and
  hqC: q \in C and
  hrC: r \in C
```

shows

```
y <= \Delta \longrightarrow |\text{fiX } f \text{ } p \text{ } r - \text{fiX } g \text{ } q \text{ } r| <= x \langle proof \rangle
```

 $\mathbf{lemma}\ abs\text{-}dif\text{-}fiX\text{-}bound\text{-}C\text{:}$

assumes

```
\begin{array}{ll} hbx \colon \forall \ l \in C. \ |f\ l - g\ l| <= x \ \mathbf{and} \\ hby1 \colon \forall \ l \in C. \ \forall \ m \in C. \ |f\ l - f\ m| <= y \ \mathbf{and} \\ hby2 \colon \forall \ l \in C. \ \forall \ m \in C. \ |g\ l - g\ m| <= y \ \mathbf{and} \\ hpC \colon p \in C \ \mathbf{and} \\ hqC \colon q \in C \ \mathbf{and} \\ hrC \colon r \in C \\ \mathbf{shows} \\ |f\! X f\ p\ r - f\! l\! X\ g\ q\ r| <= \\ x + (if\ (y <= \Delta) \ then\ \theta \ else\ y) \\ \langle proof \rangle \end{array}
```

1.3.2 Main theorem

theorem prec-enh:

```
assumes
```

1.4 Accuracy Preservation property

First, a simple lemma about an arithmetic propertie of the generalized summation over a set constructor.

```
lemma sum-div-card:

(\sum l \in \{... < n :: nat\}. \ f \ l) + q * real \ n = (\sum l \in \{... < n\}. \ f \ l + q \ )
(\mathbf{is} \ ?Sl \ n = ?Sr \ n)
\langle proof \rangle
```

Next, some lemmas about bounds that are used in the proof of Accuracy Preservation

```
\mathbf{lemma}\ bound\text{-}aux\text{-}C:
```

assumes

```
hby: \forall l \in C. \ \forall m \in C. \ |fl - fm| \le x \text{ and } hpC: p \in C \text{ and }
```

```
\begin{array}{l} hqC\colon q\!\in\! C \text{ and } \\ hrC\colon r\!\in\! C \\ \textbf{shows} \\ |f\!i\!X\,f\,p\,\,r\,-f\,\,q| <= x \\ \langle proof \rangle \\ \\ \textbf{lemma } bound\text{-}aux\colon \\ \textbf{assumes} \\ hby\colon \forall \ l\!\in\! C.\ \forall \ m\!\in\! C.\ |f\,l-f\,m| <= x \text{ and } \\ hpC\colon p\!\in\! C \text{ and } \\ hqC\colon q\!\in\! C \\ \textbf{shows} \\ |f\!i\!X\,f\,p\,\,r\,-f\,q| <= x + \Delta \\ \langle proof \rangle \end{array}
```

1.4.1 Main theorem

```
lemma accur-pres: assumes hC \colon C \subseteq PR \text{ and } \\ hby \colon \forall \ l \in C. \ \forall \ m \in C. \ |f \ l - f \ m| <= x \text{ and } \\ hpC \colon p \in C \text{ and } \\ hqC \colon q \in C \\ \text{shows} \mid cfni \ p \ f - f \ q \mid <= \\ (real \ (card \ C) * x + real \ (card \ (\{.. < np\} - C)) * (x + \Delta))/ \\ real \ np \\ (\text{is } ?abs1 <= (?bC + ?bnpC)/real \ np)
```

 \mathbf{end}

 $\langle proof \rangle$

2 Fault-tolerant Midpoint algorithm

theory LynchInstance imports Complex-Main begin

This algorithm is presented in [5].

2.1 Model of the system

The main ideas for the formalization of the system were obtained from [8].

2.1.1 Types in the formalization

The election of the basics types was based on [8]. There, the process are natural numbers and the real time and the clock readings are reals.

```
type-synonym process = nat
type-synonym time = real — real time
type-synonym Clocktime = real — time of the clock readings (clock time)
```

2.1.2 Some constants

Here we define some parameters of the algorithm that we use: the number of process and the number of lowest and highest readed values that the algorithm discards. The defined constants must satisfy this axiom. If not, the algorithm cannot obtain the maximum and minimum value, because it will have discarded all the values.

axiomatization

```
np :: nat — Number of processes and khl :: nat — Number of lowest and highest values where constants-ax: 2 * khl < np
```

We define also the set of process that the algorithm manage. This definition exist only for readability matters.

definition

```
PR :: process set where [simp]: PR = {..<np}
```

2.1.3 Convergence function

This functions is called "Fault-tolerant Midpoint" ([7])

In this algorithm each process has an array where it store the clocks readings from the others processes (including itself). We formalise that as a function from processes to clock time as [8].

First we define two functions. They take a function of clock readings and a set of processes and they return a set of khl processes which has the greater (smaller) clock readings. They were defined with the Hilbert's ε -operator (the indefinite description operator SOME in Isabelle) because in this way the formalization is not fixed to a particular election of the processes's readings to discards and then the modelization is more general.

definition

```
kmax :: (process \Rightarrow Clocktime) \Rightarrow process \ set \Rightarrow process \ set \ where
kmax \ f \ P = (SOME \ S. \ S \subseteq P \land card \ S = khl \land (\forall \ i \in S. \ \forall \ j \in (P-S). \ f \ j <= f \ i))
```

definition

```
kmin :: (process \Rightarrow Clocktime) \Rightarrow process \ set \Rightarrow process \ set \ where

kmin \ f \ P = (SOME \ S. \ S \subseteq P \land card \ S = khl \land (\forall \ i \in S. \ \forall \ j \in (P-S). \ f \ i <= f \ j))
```

With the previus functions we define a new one $reduce^1$. This take a function of clock readings and a set of processes and return de set of readings of the not dicarded processes. In order to define this function we use the image operator ((`)) of Isabelle.

¹The name of this function was taken from [5].

definition

```
reduce :: (process \Rightarrow Clocktime) \Rightarrow process \ set \Rightarrow Clocktime \ set \ \mathbf{where}
reduce \ f \ P = f \ (P - (kmax \ f \ P \cup kmin \ f \ P))
```

And finally the convergence function. This is defined with the builtin Max and Min functions of Isabelle.

definition

 $\langle proof \rangle$

```
cfnl :: process \Rightarrow (process \Rightarrow Clocktime) \Rightarrow Clocktime  where cfnl p f = (Max (reduce f PR) + Min (reduce f PR)) / 2
```

2.2 Translation Invariance property.

2.2.1 Auxiliary lemmas

These lemmas proves the existence of the maximum and minimum of the image of a set, if the set is finite and not empty.

```
lemma ex	ext{-}Maxf:
fixes S and f:: 'a \Rightarrow ('b::linorder)
assumes fin: finite S
shows S \neq \{\} ==> \exists m \in S. \ \forall s \in S. \ fs \leq fm \ \langle proof \rangle
lemma ex	ext{-}Minf:
fixes S and f:: 'a \Rightarrow ('b::linorder)
assumes fin: finite S
shows S \neq \{\} ==> \exists m \in S. \ \forall s \in S. \ fm \leq fs \ \langle proof \rangle
This trivial lemma is needed by the next two.
lemma khl	ext{-}bound: khl < np
```

The next two lemmas prove that de functions kmin and kmax return some values that satisfy their definition. This is not trivial because we need to prove the existence of these values, according to the rule of the Hilbert's operator. We will need this lemma many times because is the only thing that we know about these functions.

```
lemma kmax-prop:
fixes f :: nat \Rightarrow Clocktime
shows
(kmax f PR) \subseteq PR \land card (kmax f PR) = khl \land (\forall i \in (kmax f PR). \ \forall j \in PR - (kmax f PR). \ f j \leq f i)
\langle proof \rangle
lemma kmin-prop:
fixes f :: nat \Rightarrow Clocktime
shows
(kmin f PR) \subseteq PR \land card (kmin f PR) = khl \land
```

```
(\forall i \in (kmin \ f \ PR). \ \forall j \in PR - (kmin \ f \ PR). \ f \ i \leq f \ j) \\ \langle proof \rangle
```

The next two lemmas are trivial from the previous ones

```
lemma finite-kmax: finite (kmax f PR)
\langle proof \rangle
```

lemma finite-kmin: finite (kmin f PR)

 $\langle proof \rangle$

This lemma is necessary because the definition of the convergence function use the builtin Max and Min.

```
lemma reduce-not-empty: reduce f PR \neq \{\} \langle proof \rangle
```

The next three are the main lemmas necessary for prove the Translation Invariance property.

```
lemma reduce-shift:

fixes f :: nat \Rightarrow Clocktime

shows

f \cdot (PR - (kmax f PR \cup kmin f PR)) = f \cdot (PR - (kmax (\lambda p. f p + c) PR \cup kmin (\lambda p. f p + c) PR))

\langle proof \rangle
```

lemma max-shift: fixes $f :: nat \Rightarrow Clocktime$ and S

```
assumes notEmpFin: S \neq \{\} finite S shows Max (f'S) + x = Max ((\lambda p. f p + x) 'S) \langle proof \rangle
```

lemma min-shift:

```
fixes f :: nat \Rightarrow Clocktime and S assumes notEmpFin: S \neq \{\} finite S shows Min (f'S) + x = Min ((\lambda p. fp + x) 'S) \langle proof \rangle
```

2.2.2 Main theorem

```
theorem trans-inv:

fixes f :: nat \Rightarrow Clocktime

shows

cfnl\ p\ f + x = cfnl\ p\ (\lambda\ p.\ f\ p + x)

\langle proof \rangle
```

2.3 Precision Enhancement property

An informal proof of this theorem can be found in [6]

2.3.1 Auxiliary lemmas

This first lemma is most important for prove the property. This is a consecuence of the *card-Un-Int* lemma

 ${\bf lemma}\ pige on hole:$

assumes

```
finitA: finite A and
Bss: B \subseteq A and Css: C \subseteq A and
cardH: card A + k <= card \ B + card \ C
shows k <= card \ (B \cap C)
\langle proof \rangle
```

This lemma is a trivial consecuence of the previous one. With only this lemma we can prove the Precision Enhancement property with the bound $\pi(x,y) = x + y$. But this bound not satisfy the property

$$\pi(2\Lambda + 2\beta\rho, \delta_S + 2\rho(r_{max} + \beta) + 2\Lambda) \le \delta_S$$

that is used in [8] for prove the Schneider's schema.

lemma subsets-int:

assumes

```
\begin{array}{l} \textit{finitA: finite } A \ \mathbf{and} \\ \textit{Bss: } B \subseteq A \ \mathbf{and} \ \textit{Css: } C \subseteq A \ \mathbf{and} \\ \textit{cardH: } \textit{card } A < \textit{card } B + \textit{card } C \\ \mathbf{shows} \\ B \cap C \neq \{\} \\ \langle \textit{proof} \rangle \end{array}
```

This lemma is true because reduce f PR is the image of $PR - (kmax f) PR \cup kmin f PR$) by the function f.

$\mathbf{lemma}\ exist\text{-}reduce\text{:}$

```
\forall c \in reduce \ f \ PR. \ \exists \ i \in PR-(kmax \ f \ PR \cup kmin \ f \ PR). \ f \ i = c \ \langle proof \rangle
```

The next three lemmas are consequence of the definition of reduce, kmax and kmin

```
lemma finite-reduce:
```

```
finite (reduce f PR) \langle proof \rangle
```

lemma kmax-ge:

```
\forall \ i \in (kmax \ f \ PR). \ \forall \ r \in (reduce \ f \ PR). \ r <= f \ i \\ \langle proof \rangle
```

```
lemma kmin-le: \forall i \in (kmin \ f \ PR). \ \forall \ r \in (reduce \ f \ PR). \ f \ i <= r
```

The next lemma is used for prove the Precision Enhancement property. This has been proved in ICS. The proof is in the appendix A.1. This cannot be prove by a simple *arith* or *auto* tactic.

This lemma is true also with $\theta <= c !!$

```
lemma abs-distrib-div:

0 < (c::real) \implies |a / c - b / c| = |a - b| / c
```

The next three lemmas are about the existence of bounds of the values Max (reduce f PR) and Min (reduce f PR). These are used in the proof of the main property.

```
lemma uboundmax:
```

```
assumes
hC \colon C \subseteq PR \text{ and}
hCk \colon np <= card \ C + khl
shows
\exists \ i \in C. \ Max \ (reduce \ f \ PR) <= f \ i
\langle proof \rangle
\mathbf{lemma} \ lboundmin \colon
assumes
hC \colon C \subseteq PR \ \mathbf{and}
hCk \colon np <= card \ C + khl
shows
\exists \ i \in C. \ f \ i <= Min \ (reduce \ f \ PR)
\langle proof \rangle
\mathbf{lemma} \ same-bound \colon
```

```
assumes
```

```
hC: C \subseteq PR and hCk: np <= card \ C + khl and hnk: \ 3 * khl < np shows \exists \ i \in C. \ Min \ (reduce \ f \ PR) <= f \ i \land g \ i <= Max \ (reduce \ g \ PR) \ \langle proof \rangle
```

2.3.2 Main theorem

The most part of this theorem can be proved with CVC-lite using the three previous lemmas (appendix A.2).

```
theorem prec-enh: assumes
```

```
\begin{array}{l} hC\colon C\subseteq PR \text{ and } \\ hCF\colon np-nF<=card\ C \text{ and } \\ hFn\colon 3*nF< np \text{ and } \\ hFk\colon nF=khl \text{ and } \\ hbx\colon \forall\ l\in C.\ |f\ l-g\ l|<=x \text{ and } \\ hby1\colon \forall\ l\in C.\ \forall\ m\in C.\ |f\ l-f\ m|<=y \text{ and } \\ hby2\colon \forall\ l\in C.\ \forall\ m\in C.\ |g\ l-g\ m|<=y \text{ and } \\ hpC\colon p\in C \text{ and } \\ hqC\colon q\in C \\ \textbf{shows}\ |\ cfnl\ p\ f-cfnl\ q\ g\ |<=y\ /\ 2+x \\ \langle proof\ \rangle \end{array}
```

2.4 Accuracy Preservation property

No new lemmas are needed for prove this property. The bound has been found using the lemmas *uboundmax* and *lboundmin*

This theorem can be proved with ICS and CVC-lite assuming those lemmas (see appendix A.3).

```
theorem accur-pres: assumes hC\colon C\subseteq PR \text{ and } hCF\colon np-nF <= card\ C \text{ and } hFk\colon nF = khl \text{ and } hby\colon \forall\ l\in C.\ \forall\ m\in C.\ |f\ l-f\ m| <= y \text{ and } hqC\colon q\in C shows |\ cfnl\ p\ f-f\ q\ |<= y \ \langle proof \rangle
```

end

A CVC-lite and ICS proofs

A.1 Lemma abs_distrib_div

In the proof of the Fault-Tolerant Mid Point Algorithm we need to prove this simple lemma:

```
lemma abs-distrib-div:

0 < (c::real) \implies |a / c - b / c| = |a - b| / c
```

It is not possible to prove this lemma in Isabelle using *arith* nor *auto* tactics. Even if we added lemmas to the default simpset of HOL.

In the translation from Isabelle to ICS we need to change the division by a multiplication because this tools do not accept formulas with this arithmetic operator. Moreover, to translate the absolute value we define e constant for each application of that function. In ICS it is proved automatically.

File abs_distrib_mult.ics:

It was not possible to find the proof in CVC-lite because the formula is not linear. Two proofs where attempted. In the first one we use lambda abstraction to define the absolute value. The second one is the same translation that we do in ICS.

File abs_distrib_mult.cvc:

File abs_distrib_mult2.cvc:

A.2 Bound for Precision Enhancement property

In order to prove Precision Enhancement for Lynch's algorithm we need to prove that:

```
have |Max (reduce f PR) + Min (reduce f PR) + - Max (reduce g PR) + - Min (reduce g PR)| <= y + 2 * x
```

This is the result of the whole theorem where we multiply by two both sides of the inequality.

In order to do the proof we need to translate also the lemmas *uboundmax*, *lboundmin*, *same_bound* (lemmas about the existence of some bounds), the axiom *constants_ax* and the assumptions of the theorem.

We make five different translations. In each one we where increasing the amount of eliminated quantifiers.

File bound_prec_enh4.cvc:

Note that we leave quantifiers in some assumptions.

In the next file we also try to do the proof with all quantifiers, but CVC cannot find it.

File bound_prec_enh.cvc:

We also try to do the proof removing all quantifiers and the proof was successful.

File bound_prec_enh7.cvc:

From this last file we make the translation also for ICS adding a constant for each application of the absolute value. In this case ICS do not find the proof.

File bound_prec_enh.ics:

A.3 Accuracy Preservation property

The proof of this property was successful in both tools. Even in CVC-lite the proof was find without the need of removing the quantifiers.

File accur_pres.cvc:

File accur_pres.ics:

References

- [1] D. Barsotti, L. P. Nieto, and A. Tiu. Verication of clock synchronization algorithms: Experiments on a combination of deductive tools. In *Proceedings of AVOCS 2005*, volume 145 of *ENTCS*, pages 63–68. Elsevier Science B. V., 2005. Available by WWW from http://www.cs.famaf.unc.edu.ar/~damian/publications/clock.pdf.
- [2] CVC Lite home page. http://verify.stanford.edu/CVCL/, 2006.
- [3] ICS: Integrated Canonizer and Solver home page. http://ics.csl.sri.com/, 2006.
- [4] L. Lamport and P. M. Melliar-Smith. Synchronizing clocks in the presence of faults. *J. ACM*, 32(1):52–78, 1985.
- [5] J. Lundelius and N. Lynch. A new fault-tolerant algorithm for clock synchronization. In *PODC '84: Proceedings of the third annual ACM symposium on Principles of distributed computing*, pages 75–88, New York, NY, USA, 1984. ACM Press.
- [6] P. S. Miner. Verification of fault-tolerant clock synchronization systems. NASA Technical Paper 3349, NASA Langley Research Center, November 1993.
- [7] F. B. Schneider. Understanding protocols for Byzantine clock synchronization. Technical Report TR 87–859, Cornell University, Dept. of Computer Science, Upson Hall, Ithaca, NY 14853, 1987.
- [8] N. Shankar. Mechanical verification of a generalized protocol for byzantine fault tolerant clock synchronization. In J. Vytopil, editor, Formal Techniques in Real-Time and Fault-Tolerant Systems, volume 571 of Lecture Notes in Computer Science, pages 217–236, Nijmegen, The Netherlands, jan 1992. Springer-Verlag.